

## FORGOTTEN TOPOLOGICAL INDEX OF SUBDIVISION GRAPH AND LINE GRAPH OF GRAPHENE

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### ABSTRACT

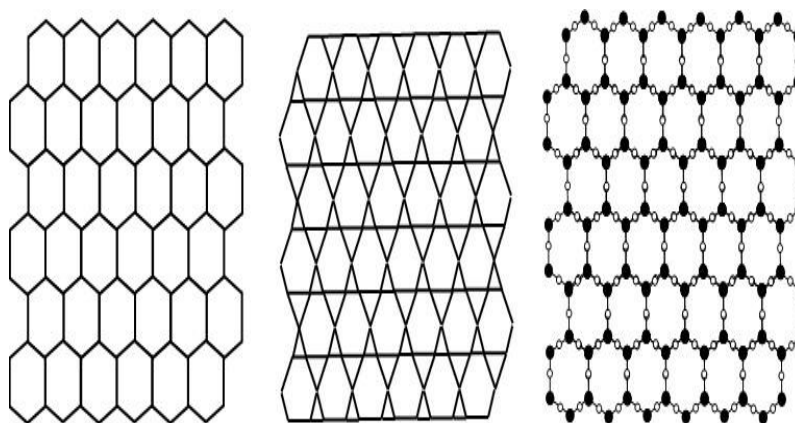
The forgotten topological index widely used in the analysis of drug molecular structures, which is helpful for pharmaceutical and medical scientists to grasp the biological and chemical characteristics of new drugs. In this paper we present the Forgotten index of subdivision graph and line graph of widely used chemical structure graphene.

**Keywords:** Forgotten topological index, line graph, subdivision graph

**Mathematics Subject Classification:** 05C07, 92E10

### I. INTRODUCTION

Development of drugs in medicine industry has more demand to determine the pharmacological, chemical and biological characteristic of these new drugs. In theoretical chemistry, chemical compounds and drugs are modeled as graphs in which each vertex represents an atom of molecule and covalent bonds between atoms are represented by edges between the corresponding vertices. Such a graph constructed according to a chemical compound is often called its molecular graph. Many previous studies have pointed out that chemical and pharmacodynamics characteristics of drugs and their molecular structures are closely correlated [2, 5, 6, 7, 9, 10]. In mathematical chemistry, numbers encoding certain structural features of organic molecules and derived from the corresponding molecular graph, are called graph invariants or more commonly topological indices. In mathematical medicine the structure of the drug is represented as an undirected graph. Where each vertex indicates an atom and each edge



**Figure 1:** 2-Dimensional graph of graphene sheet and its line graph and subdivision graph represents a chemical bond between the atoms.

Let  $G$  be a simple graph corresponding to a drug structure with vertex (atom) set  $V(G)$  and edge (bond) set  $E(G)$ . The edge between adjacent vertices  $u$  and  $v$  is denoted by  $uv$ . Thus if  $uv \in E(G)$  then  $u$  and  $v$  are adjacent in  $G$ . The degree of a vertex  $u$  denoted by  $d_G(u) = d(u)$  is the number of edges incident to  $u$ . The subdivision graph  $S(G)$  is the graph obtained from  $G$  by replacing each of its edge by a path of length 2, or equivalently, by inserting an additional vertex into each edge of  $G$ . The line graph of a graph  $G$ , denoted by  $L(G)$  is the graph whose vertices has one to one correspondence with the edges of  $G$  and two vertices in  $L(G)$  are adjacent if and only if the corresponding edges are adjacent in  $G$ . For a graph theoretic terminology, we refer the books [1, 8]. In this paper we carried out the further studies of the paper [4] and obtained forgotten index of subdivision graph and line graph of graphene.

**1. Line graph and subdivision graph of graphene**

**Theorem 2.1.** Let  $G(m,n)$  be a graphene sheet with  $n$ -rows and  $m$ -columns as in Fig.1, then

$$F[L(G(m,n))] = \begin{cases} 192mn - 2n - 20m - 140 & \text{if } n \neq 1 \\ 172m - 124 & \text{if } n = 1 \end{cases}$$

Proof. If  $n \neq 1$  then by analysis of structure of line graph of graphene sheet  $G(m,n)$  we partition the vertex set of  $L[G(m,n)]$  into three subsets as  $V_1 = \{u/d(u) = 2\}, V_2 =$

$\{u/d(u) = 3\}$  and  $V_3 = \{u/d(u) = 4\}$ . Let  $d_i$  denotes number of vertices whose the degree of vertex is  $i$ . The number of vertices on each row of line graph of graphane sheet  $G(m,n)$  is given in the Table 1. Using the data of Table 1, we can easily write that

$$|V_1| = n + 4, |V_2| = 2n + 4m - 4, |V_3| = 3mn - n - 2m - 1$$

Therefore, using the definition of forgotten topological index, we obtain

**Table 1:** Number of vertices in each row of  $L[G(m,n)]$ .

Row	$d_2$	$d_3$	$d_4$
1	3	$2(m-1)+2$	$3(m-1)+1$
2	1	2	$3m-1$
3	1	2	$3m-1$
.	.	.	.
.	.	.	.
.	.	.	.
.	.	.	.
.	.	.	.
$n-1$	1	2	$3m-1$
$n$	3	$2(m-1)+2$	$m-1$

$$\begin{aligned} F[L(G(m,n))] &= \sum_{u \in V(L[G(m,n)])} (d(u))^3 \\ &= \sum_{u \in V_1} (d(u))^3 + \sum_{u \in V_2} (d(u))^3 + \sum_{u \in V_3} (d(u))^3 \\ &= (n + 4)(8) + (2n + 4m - 4)(27) + (3mn - n - 2m - 1)(64) \\ &= 192mn - 2n - 20m - 140. \end{aligned}$$

If  $n = 1$  then by the direct observation,  $|V_1| = 6, |V_2| = 4(m - 1), |V_3| = n - 1$ , the forgotten index of  $L[G(m,n)]$  when  $n=1$  is

$$F[L(G(m,n))] = 172m - 124.$$

**Theorem 2.2.** Let  $G(m,n)$  be a graphene sheet with  $n$ -rows and  $m$ -columns as in Fig.1, then we obtain

$$F[S(G(m,n))] = \begin{cases} 78mn + 32m + 32n - 46 & \text{if } n \neq 1 \\ 110m - 14 & \text{if } n = 1 \end{cases}$$

Proof. If  $n = 1$  and  $m \geq 1$ , then we get the result by putting  $n = 1$  in case (i). Now for  $n \geq 2$  and  $m \geq 1$ , by analysis of structure of line graph of graphene sheet  $G(m,n)$ , we partition the vertex set of  $S[G(m,n)]$  into two subsets as  $V_1 = \{u/d(u) = 2\}$  and  $V_2 = \{u/d(u) = 3\}$ . The number of vertices on each row of line graph of graphane sheet  $S[G(m,n)]$  is given in the Table 1. Using the data of Table 2, we can easily write that

$$|V_1| = 3mn + 4m + 4n + 1 \text{ and } |V_2| = 2mn - 2$$

**Table 2:** Number of vertices in each row of  $G(m,n)$ .

Row	$d_2$	$d_3$
1	$6m+4$	$3m-1$

2	3m+4	2m
3	3m+4	2m
.	.	.
.	.	.
.	.	.
.	.	.
.	.	.
n-1	3m+4	2m
n	4m+5	m-1

Therefore, using the definition of forgotten topological index, we obtain

$$\begin{aligned}
 F[S(G(m,n))] &= \sum_{u \in V(L(G(m,n)))} (d(u))^3 \\
 &= \sum_{u \in V_1} (d(u))^3 + \sum_{u \in V_2} (d(u))^3 \\
 &= (3mn + 4m + 4n + 1)(8) + (2mn - 2)(27) \\
 &= 78mn + 32m + 32n - 46.
 \end{aligned}$$

If  $n = 1$  then by the direct observation, we have

$$F[L(G(m,n))] = 110m - 14.$$

## II. CONCLUSION

In this work, we obtain forgotten topological index of subdivision graph and line graph of graphene structure which is widely used in pharmaceutical field. Further, one can obtain the other topological index of this structure and can establish the other properties of graphene structure with usage of topological indices.

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